

Name _____ Period _____

Area of Parallelograms, Triangles, and Trapezoids

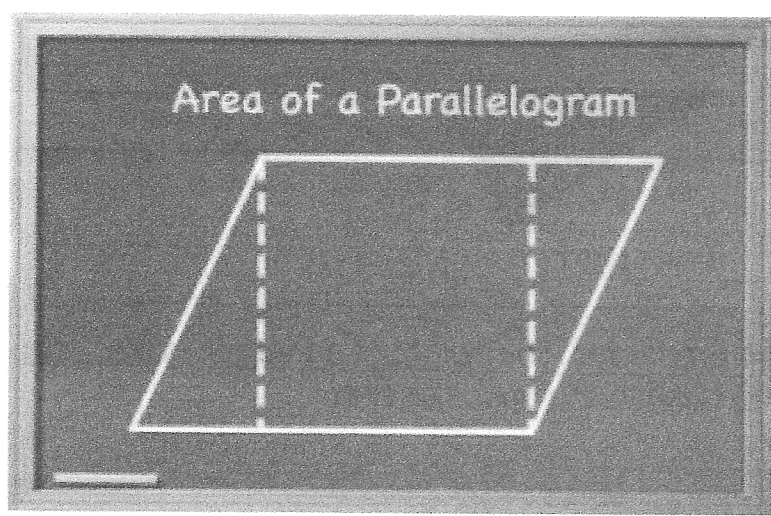
All three of these figures have formulas with one thing in common:

_____ X _____

For all three figures, the _____ must always be a _____
line from the _____.

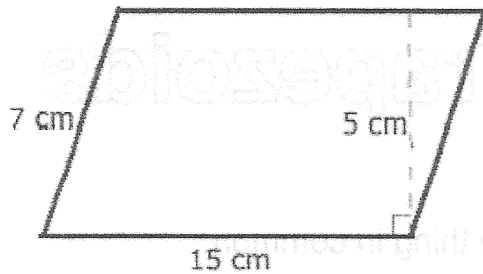
The formula for the area of a parallelogram is _____ x _____
because a parallelogram has the same area as a rectangle with the same
height and base.

Proof:



Find the area of the parallelogram:

Example 1:

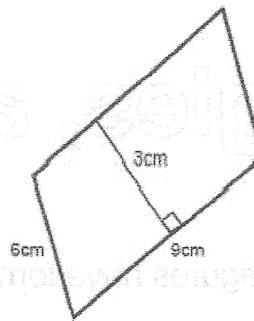


$$A = bh$$

$$A = \underline{\quad} \times \underline{\quad}$$

$$A = \underline{\quad} \text{ cm squared}$$

Example 2:



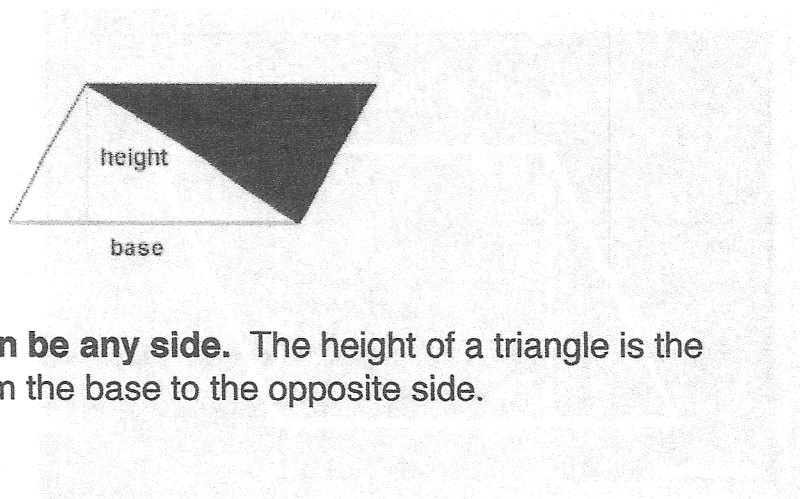
$$A = bh$$

$$A = \underline{\quad} \times \underline{\quad}$$

$$A = \underline{\quad} \text{ cm squared}$$

Now we need to find the area of triangles and trapezoids.

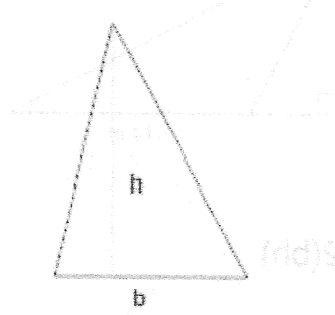
When looking at a parallelogram, we notice that the diagonal of a parallelogram divides the parallelogram into two congruent triangles. Therefore, the area of each triangle is half the area of the parallelogram.



The base of a triangle can be any side. The height of a triangle is the perpendicular distance from the base to the opposite side.

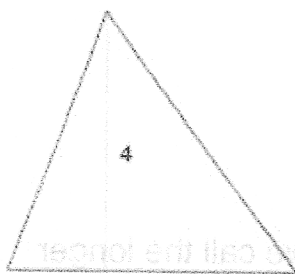
Here is a chart to help you understand how to find the area of a triangle, along with a picture to help you learn.

AREA OF A TRIANGLE

<p>The area A of a triangle is half the product of its base b and its height h.</p>	$A = \frac{1}{2}bh$	
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Now that we know how to find the area of a triangle, let's do an example together!

Example 1: Find the area of the triangle.



We use the formula and substitute for l and w .

$$A = \frac{1}{2}(bh)$$

$$A = \underline{\hspace{2cm}} \times \underline{\hspace{2cm}} \times \underline{\hspace{2cm}}$$

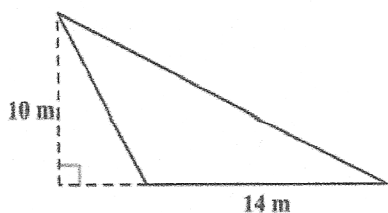
$$A = \underline{\hspace{2cm}} \text{ square units}$$



- Note: Our units are in square units. We do not have a specific unit of measurement to use, so we assume the measurement to be in units.

There is a chart to help you understand how to find the area of a triangle, along with a picture to help you learn.

Example 2:



AREA OF A TRIANGLE

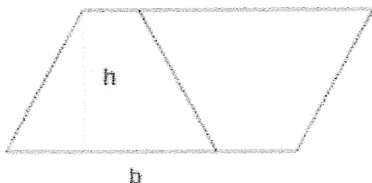
The area A of a triangle is half the product of its base b and its height h .

$A = \frac{1}{2}(bh)$

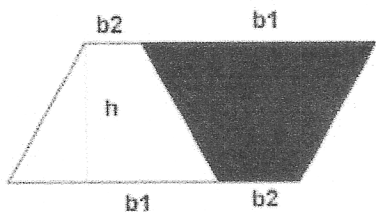
$A = \underline{\hspace{2cm}} \times \underline{\hspace{2cm}} \times \underline{\hspace{2cm}}$

$A = \underline{\hspace{2cm}}$ square meters

A parallelogram can be divided into two congruent trapezoids. The area of each trapezoid is one-half the area of the parallelogram.



The two parallel sides of a trapezoid are its bases. If we call the longer side b_1 and the shorter side b_2 , then the base of the parallelogram is $b_1 + b_2$.



We use the formula and substitute for h and w .

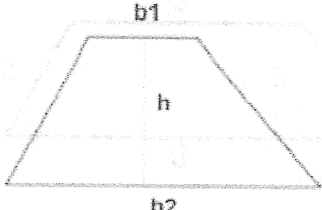
$A = \frac{1}{2}(b_1 + b_2)h$

$A = \underline{\hspace{2cm}} \times \underline{\hspace{2cm}} \times \underline{\hspace{2cm}}$

$A = \underline{\hspace{2cm}}$ square units

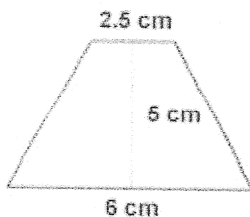
Notes: Our units are in square units. We do not have a specific unit of measurement to use, so we assume the measurement to be in units.

AREA OF A TRAPEZOID

<p>The area A of a trapezoid is half its height multiplied by the sum of the lengths of its two bases.</p>	$A = \frac{1}{2}h(b_1 + b_2)$	
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The only difference between the formulas for _____ and _____ is the _____. A trapezoid has 2 _____ different size _____. They must be _____ together, _____ by the _____, and _____ by $\frac{1}{2}$.

Example 1: Find the area of the trapezoid.

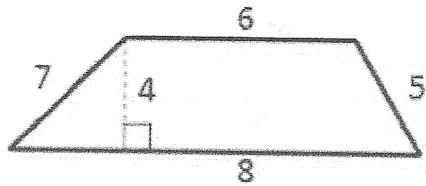


$$A = \frac{1}{2}h(b_1 + b_2)$$

$$A = \underline{\hspace{2cm}} \times \underline{\hspace{2cm}} \times (\underline{\hspace{2cm}} + \underline{\hspace{2cm}})$$

$$A = \underline{\hspace{2cm}} \text{ cm squared}$$

Example 2:

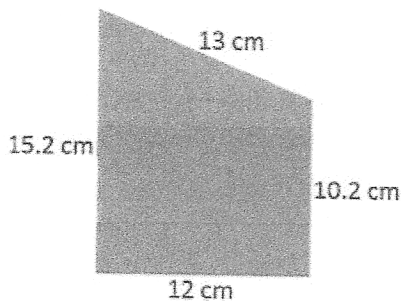


$$A = \frac{1}{2}h(b_1 + b_2)$$

$$A = \underline{\quad} \times \underline{\quad} \times (\underline{\quad} + \underline{\quad})$$

$$A = \underline{\quad} \text{ square units}$$

Example 3:



$$A = \frac{1}{2}h(b_1 + b_2)$$

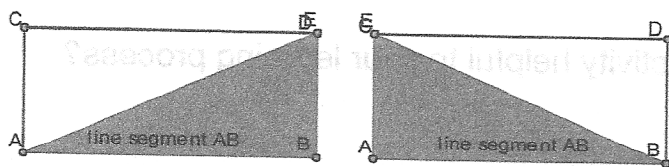
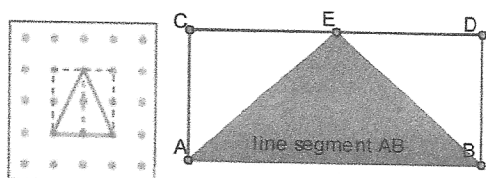
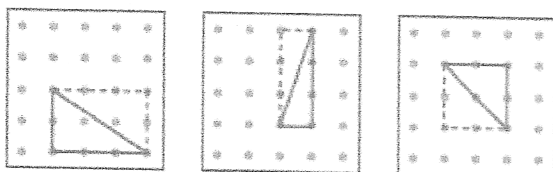
$$A = \underline{\quad} \times \underline{\quad} \times (\underline{\quad} + \underline{\quad})$$

$$A = \underline{\quad} \text{ cm squared}$$

Now that we know how to find the area of a triangle and the area of a trapezoid, let's do an activity utilizing the new concepts that we have just learned.

Activity: Tell how to use the area of a right triangle to find the area of a trapezoid.

- Draw a triangle (with the use of a ruler) with whole number side lengths. Fit the triangle on a piece of graph paper.
- Now cut out the triangle and use the formula, $A = \frac{1}{2} bh$, to show that any of the three sides can serve as the base of the triangle.
- In order to find the height, draw a rectangle around the cutout triangle on another sheet of graph paper to find the height of the triangle for each base.



Calculations:

Write responses to the following questions:

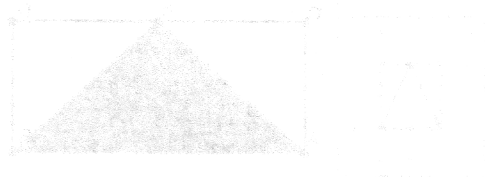
- Tell how to use the sides of a right triangle to find its area.

Draw a triangle (with the use of a ruler) with whole number side lengths. Fit the triangle on a piece of graph paper. Now cut out the triangle and use the formula $A = \frac{1}{2}bh$ to show that any of the three sides can serve as the base of the triangle.

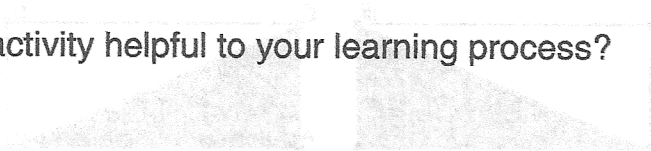
- Explain how to find the area of a trapezoid.



- How is the trapezoid area formula similar to the triangle area formula



- How is this particular activity helpful to your learning process?



Calculations