

Name \_\_\_\_\_ Period \_\_\_\_\_

# Factoring

A working definition of factoring is: \_\_\_\_\_.

The first step in any factoring problem is to \_\_\_\_\_.

This means to use the \_\_\_\_\_ in reverse.

## EXAMPLES OF DISTRIBUTIVE PROPERTY

$$6(x + 7) = 6x + 42$$

$$7(2x + 3) = 14x + 21$$

$$9(x - 4) = 9x - 36$$

$$12(2x + 1) = 24x + 12$$

$$5(3x - 2y + 4) = 15x - 10y + 20$$

$$5x(x + 4) = 5x^2 + 20x$$

## EXAMPLES OF FACTORING

$$6x + 42 = 6(x + 7)$$

$$14x + 21 = 7(2x + 3)$$

$$9x - 36 = 9(x - 4)$$

$$24x + 12 = 12(2x + 1)$$

$$15x - 10y + 20 = 5(3x - 2y + 4)$$

$$5x^2 + 20x = 5x(x + 4)$$

When \_\_\_\_\_ the common factor, look for a number or variable that \_\_\_\_\_ into both (or all) terms. If there is more than one common factor, be sure to get the \_\_\_\_\_.

**Example 1:**  $12x + 36$

Solution:

1. There are several numbers that divide evenly into both 12 and 36: \_\_\_\_\_.
2. Take the largest common factor, which is \_\_\_\_\_.
3. Write down the 12, then \_\_\_\_\_:  $12( \quad + \quad )$ .
4. In the parentheses you put the \_\_\_\_\_, x and 3, like this:

$$12x + 36 = 3(x + 3)$$

**EXERCISES: Factor completely.**

$$1.3 \overline{) 3x + 15}$$

$$= 3(x + 5)$$

$$2.8 \overline{) 8x + 24}$$

$$= 8(x + 3)$$

$$3. 7x - 28$$

$$= \underline{\hspace{1cm}} (\underline{\hspace{1cm}} - \underline{\hspace{1cm}})$$

$$4. 5x - 25$$

$$= \underline{\hspace{1cm}} (\underline{\hspace{1cm}} - \underline{\hspace{1cm}})$$

$$5. 34x + 17y$$

$$= 17(\underline{\hspace{1cm}})$$

$$6. 14x + 28y$$

$$= \underline{\hspace{1cm}} (\underline{\hspace{1cm}})$$

$$7. 12x + 36y$$

$$= \underline{\hspace{1cm}} (\underline{\hspace{1cm}})$$

$$8. 15x + 60y$$

$$= \underline{\hspace{1cm}} (\underline{\hspace{1cm}})$$

$$9. 7x + 7$$

$$= \underline{\hspace{1cm}} (\underline{\hspace{1cm}} + 1)$$

$$10. 3x^2 + 3$$

$$= 3(\underline{\hspace{1cm}} + \underline{\hspace{1cm}})$$

$$11. 42x^2 + 21$$

$$= 21(\underline{\hspace{1cm}})$$

$$12. 30x^2 + 15$$

$$= \underline{\hspace{1cm}} (\underline{\hspace{1cm}})$$

$$13. 5x^2 + 15x$$

$$= 5x(x + \underline{\hspace{1cm}})$$

$$14. 7x^2 + 21x$$

$$= 7x(\underline{\hspace{1cm}})$$

$$15. 7x^2 + 14x$$

$$= \underline{\hspace{1cm}} (\underline{\hspace{1cm}})$$

$$16. 7x^2 - 14x$$

$$= \underline{\hspace{1cm}} (\underline{\hspace{1cm}})$$

$$17. 3x^2 + 12x$$

$$= \underline{\hspace{1cm}} (\underline{\hspace{1cm}})$$

$$18. 21x^2 + 30x$$

$$= \underline{\hspace{1cm}} (\underline{\hspace{1cm}})$$

$$19. 16x^2 - 18x$$

$$= \underline{\hspace{1cm}} (\underline{\hspace{1cm}})$$

$$20. 12x^2 - 30x$$

$$= \underline{\hspace{1cm}} (\underline{\hspace{1cm}})$$

$$21. x^3 + 3x^2$$

$$= x^2(\underline{\hspace{1cm}})$$

$$22. x^3 + 4x^2$$

$$= \underline{\hspace{1cm}}$$

$$23. x^3 + 4x$$

$$= \underline{\hspace{1cm}}$$

$$24. x^3 - 4x^2$$

$$= \underline{\hspace{1cm}}$$

$$25. 4x^3 + 8x^2 \\ = 4x^2( \quad )$$

$$26. 4x^3 + 8x \\ = 4x( \quad )$$

$$27. 12x^3 - 8x^2 \\ = \underline{\hspace{2cm}}$$

$$28. 16x^3 - 24x^2 \\ = 8x^2( \quad )$$

$$29. 16x^3 + 32x^2 \\ = \underline{\hspace{1cm}}( \quad )$$

$$30. 12x^3 + 18x^2 \\ = \underline{\hspace{2cm}}$$

$$31. 12x^3 - 18x^2 \\ = \underline{\hspace{2cm}}$$

$$32. 45x^3 + 30x^2 \\ = \underline{\hspace{2cm}}$$

$$33. 12x^2 + 12 \\ = \underline{\hspace{2cm}}$$

$$34. 24x^2 + 12 \\ = \underline{\hspace{2cm}}$$

$$35. 24x^2 + 12x \\ = \underline{\hspace{2cm}}$$

$$36. 144x^2 + 12x \\ = \underline{\hspace{2cm}}$$

$$37. 16x^2 + 48x^3 \\ = 16x^2( \quad )$$

$$38. 16x^2 - 48x^3 \\ = \underline{\hspace{2cm}}$$

$$39. 24x^4 + 36x^3 \\ = \underline{\hspace{2cm}}$$

$$40. 24x^3 + 24x^2 \\ = \underline{\hspace{2cm}}$$

$$41. 24x^3 + 24x \\ = \underline{\hspace{2cm}}$$

$$42. 24x^4 + 16x^2 \\ = \underline{\hspace{2cm}}$$

$$43. 6x + 9y - 12 \\ = 3( \underline{\hspace{1cm}} + \underline{\hspace{1cm}} - \underline{\hspace{1cm}} )$$

$$44. 3x + 6y + 12z \\ = \underline{\hspace{1cm}}( \quad )$$

$$45. 9x + 18y + 9 \\ = 9( \quad )$$

$$46. 30x + 20y + 10 \\ = 10( \underline{\hspace{1cm}} + \underline{\hspace{1cm}} + \underline{\hspace{1cm}} )$$

$$47. 30x + 20y - 5 \\ = \underline{\hspace{2cm}}$$

$$48. 35x + 28y - 14z \\ = \underline{\hspace{2cm}}$$

$$49. 30x^2 + 20xy - 10y^2 \\ = \underline{\hspace{2cm}}$$

$$50. 30x^3 + 20xy + 10x^2 \\ = \underline{\hspace{2cm}}$$

$$51. 12x^3 + 24x^2 + 24x \\ = \underline{\hspace{2cm}}$$

$$52. 12x^3 - 24x^2 + 3x \\ = \underline{\hspace{2cm}}$$

$$53. 19x^3 + 19x^2y + 38x^2$$

$$= \underline{\hspace{4cm}}$$

$$54. 36x^3 + 24x^2y + 12x^2$$

$$= \underline{\hspace{4cm}}$$

$$55. 16x^2 + 32x^3$$

$$= 16x^2(\quad)$$

$$56. 16x^3 + 32x^2$$

$$= \underline{\hspace{4cm}}$$

$$57. 16x^3 - 12x^2$$

$$= \underline{\hspace{4cm}}$$

$$58. 16x^3 - 12x^2$$

$$= \underline{\hspace{4cm}}$$

$$59. y^5 - 14y^3$$

$$= y^3(\quad)$$

$$60. x^{10} + 5x^3$$

$$= x^3(\quad)$$

From exercises #55 - 60 above, observe the rule listed below!

**RULE**

When factoring powers, take out the *lowest* exponent (power) of the factor. Then *subtract* exponents.

$$61. 16x^2y^3 - 12x^3y^2$$

$$= 4x^2y^2(\quad)$$

$$62. 4x^3y^3 + 8x^2y^4$$

$$= 4x^2y^3(\quad)$$

$$63. 5x^3y^3 + 10x^2y$$

$$= \underline{\hspace{4cm}}$$

$$64. 8x^5y^2 - 16x^4y^3$$

$$= \underline{\hspace{4cm}}$$

$$65. 8x^5y^3 + 12x^3y^4$$

$$= \underline{\hspace{4cm}}$$

$$66. 8x^3y^4 + 24x^2y^6$$

$$= \underline{\hspace{4cm}}$$

When an expression contains negative terms, it is sometimes helpful to be able to factor out the negative or to factor out a “-1.” If you factor out a “-1”, this changes each sign inside the parentheses that follow, as in the following example.

**EXAMPLE 2.** Factor out a “-1” from the expression  $-4x - 6y + 9$ .

**Solution:**  $-4x - 6y + 9 = -1(4x + 6y - 9)$  or  
 $= -(4x + 6y - 9)$  You can verify by the distributive property!

**EXERCISES.** In each of the following, factor completely, including the “negative.”

67.  $-x^2 - 4x + 6$   
 $= -1( \quad + \quad - \quad )$   
 or  $-( \quad + \quad - \quad )$

68.  $-x^2 + 5x - 1$   
 $= -1( \quad \quad \quad )$   
 or  $-( \quad \quad \quad )$

69.  $-x^2 + 3x + 7$   
 $= \underline{\hspace{2cm}}$

70.  $-6x^2 + 12$   
 $= -6( \quad \quad \quad )$

71.  $-6x - 9y + 15$   
 $= -3( \quad \quad \quad )$

72.  $-8x + 20y - 24$   
 $= \underline{\hspace{2cm}}$

73.  $-x^2 - 4x$   
 $= -x( \quad \quad \quad )$

74.  $-x^2 - 7x$   
 $= \underline{\hspace{2cm}}$

75.  $-x^2 + 7x$   
 $= \underline{\hspace{2cm}}$

76.  $-4x + 12x^2$   
 $= -4x(1 - \underline{\hspace{1cm}})$

77.  $-8x - 12x^2$   
 $= \underline{\hspace{2cm}}$

78.  $-4x^2 - 4y^2$   
 $= \underline{\hspace{2cm}}$

79.  $-x^2 - 3x + 8xy$   
 $= \underline{\hspace{2cm}}$

80.  $-4x^2 - 16x + 16$   
 $= \underline{\hspace{2cm}}$

81.  $-8 + 8x - x^2$   
 $= \underline{\hspace{2cm}}$

82.  $-8 - 8x - 8x^2$   
 $= \underline{\hspace{2cm}}$

83.  $8 - 16x - 40x^2$   
 $= \underline{\hspace{2cm}}$

84.  $35 + 20x - 5x^2$   
 $= \underline{\hspace{2cm}}$

In each of the following exercises, factor the common factors. As you do, observe how you move from the simple to the more complicated; from the concrete to the abstract.

85a)  $yx + 7x$

$= x ( \quad )$

b)  $ya + 7a$

$= a ( \quad )$

c)  $y\$ + 7\$$

$= \$ ( \quad )$

d)  $y(\text{Junk}) + 7(\text{Junk})$

$= (\text{Junk}) ( \quad )$

e)  $y(x+4) + 7(x+4)$

$= (x+4) ( \quad )$

86a)  $4xy + 3y$

$= \underline{\hspace{2cm}}$

b)  $4xa + 3a$

$= \underline{\hspace{2cm}}$

c)  $4x\$ + 3\$$

$= \underline{\hspace{2cm}}$

d)  $4x(\text{Junk}) + 3(\text{Junk})$

$= \underline{\hspace{2cm}}$

e)  $4x(y-7) + 3(y-7)$

$=$